

supporting: "The Illustrated Principles of Pool and Billiards" <u>http://billiards.colostate.edu</u> by David G. Alciatore, PhD, PE ("Dr. Dave")

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For "gearing" outside English, the sliding velocity of the point of contact between the cue ball and object ball must be 0, so:

$$\mathbf{v}_{\mathbf{C}} = \mathbf{v} \cdot \sin(\mathbf{\phi}) - \mathbf{\omega} \cdot \mathbf{R} = 0 \tag{1}$$

where R is the radius of the cue ball. So, using the definition of spin-rate factor (SRF) from TP A.12,

$$SRF = \frac{\omega}{\left(\frac{v}{R}\right)} = \sin(\phi)$$
(2)

From TP A.25, the percent English required to achieve this SRF is:

$$PE = \frac{4}{5} \cdot SRF \cdot 100\% = \frac{4}{5} \cdot \sin(\phi) \cdot 100\%$$
(3)

The following plot summarizes how much English is required for "gearing" outside English for various cut angles:

$$\phi := 0 \cdot \deg, 1 \cdot \deg \dots 90 \cdot \deg$$
$$\operatorname{PEg}(\phi) := \frac{4}{5} \cdot \sin(\phi) \cdot 100\%$$



For a half-ball hit:

 $\phi := 30 \cdot \deg$   $PEg(\phi) = 40 \cdot \%$ 

So, with a half-ball hit, anything less than 40% English will be less than "gearing" and will throw the OB to the right, and anything more than 40% English will result in excess outside English, causing throw to the left.

Here are the percentage-english amounts required for other standard ball-hit fractions:

	from TP 1.23:	$\oint(f) := asin(1 - f)$	$f(\phi) \coloneqq 1 - \sin(\phi)$
f= 0	f = 0.%	$\phi(f) = 90 \cdot \deg$	$PEg(\phi(f)) = 80.\%$
$f_{\text{m}} = \frac{1}{4}$	$f = 25 \cdot \%$	$\phi(f) = 48.59 \cdot \text{deg}$	$PEg(\phi(f)) = 60.\%$
$f_{\text{M}} = \frac{1}{2}$	f = 50.%	$\phi(f) = 30 \cdot \deg$	$PEg(\phi(f)) = 40.\%$
$f_{\text{M}} = \frac{3}{4}$	$f = 75 \cdot \%$	$\phi(f) = 14.478 \cdot \text{deg}$	$PEg(\phi(f)) = 20.\%$
f.:= 1	f = 100·%	$\phi(f) = 0 \cdot \deg$	$PEg(\phi(f)) = 0.\%$

From the data and equations above, it is clear that the percentage english required for gearing outside english (no throw) is 80% of 1 minus the ball-hit fraction:

$$PEg = 0.8 \cdot (1 - f)$$

It is easy to visualize the amount of tip offset needed to create gearing outside English for any cut angle using the technique described and illustrated below.

From Equation 3 in TP A.12, and Equation 2 above, the tip offset (x) required for gearing outside English is:

$$x = \frac{2}{5} \cdot R \cdot SPF = \frac{2}{5} R \cdot \sin(\phi) = \frac{2}{5} \cdot R \cdot \left(\frac{L}{R}\right) = \frac{2}{5} \cdot L$$

where L is the distance between the line of aim and the line-of-centers point (see the diagram at the top of this document and the diagram below). Therefore, the required tip offset is 40% (2/5) of the distance from the aiming line to the line-of-centers point on the front of the CB. The following diagram illustrates how this technique is applied at the table:

