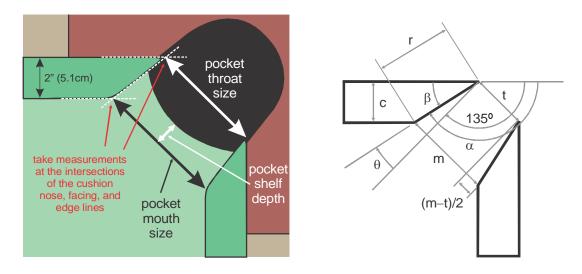




TP B.15 Pocket geometry calculations

supporting: "The Illustrated Principles of Pool and Billiards" <u>http://billiards.colostate.edu</u> by David G. Alciatore, PhD, PE ("Dr. Dave")

originally posted: 7/12/2013 last revision: 7/12/2013



The pocket facing angle is usually specified as angle $\boldsymbol{\alpha}.$

The wedge angle of the cushion is given by:

$$\beta = 180 \deg - \alpha \tag{1}$$

The angle of the facing relative to the pocket centerline is:

$$\theta = \alpha - 135 \deg$$
 (2)

These angles are also related by:

$$3 = 45 \cdot \deg - \theta \tag{3}$$

From the triangle formed by angle θ , the length of the pocket facing is:

$$r = \frac{c}{\sin(\beta)} \tag{4}$$

and the mouth-throat difference is related to this length according to:

$$\frac{(m-t)}{2} = r \cdot \sin(\theta)$$
(5)

Substituting Equation 4 into Equation 5, gives:

$$\frac{(m-t)}{2 \cdot c} \cdot \sin(\beta) = \sin(\theta)$$
(6)

But from Equation 3 and the angle-difference trig identity,

$$\sin(\beta) = \sin(45 \cdot \deg - \theta) = \sin(45 \cdot \deg) \cos(\theta) - \cos(45 \cdot \deg) \sin(\theta) = \frac{1}{\sqrt{2}} \cdot (\cos(\theta) - \sin(\theta))$$
(7)

Using Equation 7 in Equation 6 gives:

$$\frac{(m-t)}{2\cdot\sqrt{2}\cdot c} \cdot (\cos(\theta) - \sin(\theta)) = \sin(\theta)$$
(8)

Rearranging gives:

$$\tan(\theta) = \frac{\sin(\theta)}{\cos(\theta)} = \frac{1}{\left[1 + \frac{2 \cdot \sqrt{2} \cdot c}{(m-t)}\right]}$$
(9)

Therefore, from Equation 2 and 9, the facing angle can be found from the mouth-throat difference with:

$$\alpha = 135 \cdot \deg + \operatorname{atan}\left[\frac{1}{\left[1 + \frac{2 \cdot \sqrt{2} \cdot c}{(m-t)}\right]}\right]$$
(10)

Here is an example of using Equation 10 to calculate the pocketing facing angle from pocket measurements:

$$m := 4.5 \cdot \text{in} \qquad t := 3.75 \cdot \text{in} \qquad m - t = 0.75 \text{ in} \qquad c := 2 \cdot \text{in}$$
$$\alpha := 135 \cdot \text{deg} + \text{atan} \left[\frac{1}{\left[1 + \frac{2 \cdot \sqrt{2} \cdot c}{(m - t)} \right]} \right]$$

For a given pocket facing angle, the mouth-throat difference (mt) can be found using Equations 1, 2, 4 and 5:

$$\alpha := 142 \cdot \deg$$
 $c := 2 \cdot in$

$$mt := 2 \frac{c}{\sin(180 \cdot \deg - \alpha)} \cdot \sin(\alpha - 135 \cdot \deg)$$